

2019强网杯crypto writeup

原创

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本文链接：<https://blog.csdn.net/a16511232/article/details/90615866>

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本次write包含以下题目

- copperstudy
- randomstudy
- 强网先锋-辅助

copperstudy

题目描述

nc 119.3.245.36 12345

连上去返回

```
[+]proof: skr=os.urandom(8)
[+]hashlib.sha256(skr).hexdigest()=1651d7f27f35e8f177633a014dbc4eb04a99e74c09a7545d1c1f08e0f8b7f7c3
[+]skr[0:5].encode('hex')=58d0f5f7fc
[-]skr.encode('hex')=
```

破解一个原文8个字符的sha256，已知前5个字符

可以使用hashcat爆破比较快(10秒内)，也可以自己写python破解

```
#python3
#path修改为本地hashcat文件夹路径
import os
path="D:\\hashcat-5.1.0\\"
str1=input("[+]hashlib.sha256(skr).hexdigest()=")
str2=input("[+]skr[0:5].encode('hex')=")
print(path+"hashcat64.exe -a 3 --hex-salt -m 1420 {str1}:{str2} --potfile-disable ?b?b?b -o res.txt --out
os.chdir(path)
os.system(path+"hashcat64.exe -a 3 --hex-salt -m 1420 {str1}:{str2} --potfile-disable ?b?b?b -o res.txt -
with open(path+"res.txt", 'r') as f:
    lines = f.readlines()
    last_line = lines[-1]
    #print(last_line)
    if(last_line[0:4]=="$HEX"):
        print(str2+last_line[5:11])
    else:
        print(str2+hex(last_line))
```

第一问

```
[+]Generating challenge 1
[+]n=0x20918380c97c52ae96b53b371e822a972927d4cc96e1659a52ff4ba6849fd16856959ae83a91d2c0775fb06de75c5117c82f
[+]e=3
[+]m=random.getrandbits(512)
[+]c=pow(m,e,n)=0x1e494321effffbf32beebe37f042db1baeb12f42740ffe43c8b7d8e18b79170208231610e8f2f65ff85e8f5c
[+](m>>72)<<72)=0x258aa871ef627602f03f2100efe0c045d4a307153ca71f26e22fc2bcb72a16ae695d5bad767d258aa42e02a5
[-]long_to_bytes(m).encode('hex')
```

一开始没有思路，看到题目叫做copperstudy，搜索关键字ctf rsa copper，果然搜出东西，有一位叫Coppersmith对RSA提出了很多种攻击算法。

题外话，搜索是有技巧的，通常题目的解法不是第一次出现，利用题目的标题/hint/部分关键代码，加上ctf或writeup关键字，通常能搜到点有用的东西。

参考链接

[强网杯2018 - nexrsa - Writeup](#)

[CTF中常见的RSA相关问题总结](#)

[RSA大礼包（二）Coppersmith 相关](#)

第一问的解法

coppersmith攻击，已知m的高位

```
#sage脚本
load("coppersmith.sage")
N = #N的值
e = 3 #e的值
m = #m的大概值
c = #c的值
ZmodN = Zmod(N)
P. = PolynomialRing(ZmodN)
f = (m + x)^e - c
dd = f.degree()
beta = 1
epsilon = beta / 7
mm = ceil(beta**2 / (dd * epsilon))
tt = floor(dd * mm * ((1/beta) - 1))
XX = ceil(N**((beta**2/dd) - epsilon))
roots = coppersmith_howgrave_univariate(f, N, beta, mm, tt, XX)
```

第二问

```
[+++++]challenge 1 completed[+++++]
[+]Generating challenge 2
[+]n=0x4ac5cbf84a2f9a1042c552c77075459d2273994453caea11fbf696b9a8d41937b48be43c71ec6c37470ba9d280a23301b817
[+]e=65537
[+]m=random.getrandbits(512)
[+]c=pow(m,e,n)=0x19304208b44ce0bf457d757e368edde74922e89a51290937a386cb320e9c59bb80f77c4a4f1d1b0699593dc1c
[+](p>>128)<<128)=0x80f7a73798f638d10180223d7b482035b69b51ffe09ad9e42602cc9d489837be7d1ac92e90b09837144c12
```

还是coppersmith攻击，已知因子p的高位


```

#sage脚本
def partial_p(p0, kbits, n):
    PR.<x> = PolynomialRing(Zmod(n))
    nbits = n.nbits()

    f = 2^kbits*x + p0
    f = f.monic()
    roots = f.small_roots(X=2^(nbits//2-kbits), beta=0.3) # find root = n^0.3
    if roots:
        x0 = roots[0]
        p = gcd(2^kbits*x0 + p0, n)
        return ZZ(p)

def find_p(d0, kbits, e, n):
    X = var('X')

    for k in xrange(1, e+1):
        results = solve_mod([e*d0*X - k*X*(n-X+1) + k*n == X], 2^kbits)
        for x in results:
            p0 = ZZ(x[0])
            p = partial_p(p0, kbits, n)
            if p:
                return p

n = 0x6076ea10cc4cef8ceb867f3958946426d25fb06a9d3192d55390bd5611664432bf57d8e2c50cbb897e6086d185145b0af11ea
e = 3
d = 0xfd7a028dfde00006c3c94b076e29b9786800722872f5ffabe50df2eac3766d801903baafa26eab26e5aa7c90a7d0540d43cdb

beta = 0.5
epsilon = beta^2/7

nbits = n.nbits()
kbits = 511
d0 = d & (2^kbits-1)
print "lower %d bits (of %d bits) is given" % (kbits, nbits)

p = find_p(d0, kbits, e, n)
print "found d: %d" % p
q = n//p
print d
print inverse_mod(e, (p-1)*(q-1))

```

第四问

```

[+++++]challenge 3 completed[+++++]
[+]Generating challenge 4
[+]e=3
[+]m=random.getrandbits(512)
[+]n1=0x8782029df97597a52ae2657b3e2bd6e13abb98c66c232b58ebaf4a0840e21d92a3d2c96d2168bcf6e23a2e7ac21438ee331
[+]c1=pow(m,e,n1)=0x44ae824c4704561e3d726ec074ed549b00873d2332e40619ed7b986f467d032e536e3be84a801026aa9d830
[+]n2=0x28abc38a463248ed10564e1709a8c4345d5a0b627d5fa608e9c7280d1aa60f209ff179fd4e7298e4c39ed9539a06103317
[+]c2=pow(m,e,n2)=0x1dfcfb67c84c6a0a701aacbc429b3d67ba804bd9d8401a1e9b46f7ff4f20cc94f6156d71128bc081ad9e45
[+]n3=0x3c2a8de96e6e1b8f15c9b01abfd3027d78eef0c77396cd1e676afc0a4ba0e3ba6b194387e0fbed1296bf523222e4aa43c
[+]c3=pow(m,e,n3)=0x16c7c51ebd1e420ef58c4c675c0528043f021af620e0e57cc781714c737684df21782295fc343d44a52b938
[-]long_to_bytes(m).encode('hex')=

```

同一个密文m，使用相同的较小的e=3，不同的n加密
低加密指数广播攻击

```
#python
from gmpy2 import invert, iroot
e=3
n1=0x8782029df97597a52ae2657b3e2bd6e13abb98c66c232b58ebaf4a0840e21d92a3d2c96d2168bcf6e23a2e7ac21438ee331961
c1=0x44ae824c4704561e3d726ec074ed549b00873d2332e40619ed7b986f467d032e536e3be84a801026aa9d830a999c3bb56a694d
n2=0x28abcfc38a463248ed10564e1709a8c4345d5a0b627d5fa608e9c7280d1aa60f209ff179fd4e7298e4c39ed9539a06103317405
c2=0x1dfcfcfb67c84c6a0a701aaacbc429b3d67ba804bd9d8401a1e9b46f7ff4f20cc94f6156d71128bc081ad9e457fc9fba53cda2c2
n3=0x3c2a8de96e6e1b8f15c9b01abfd3027d78eef0c77396cd1e676afc0a4ba0e3ba6b194387e0fbed1296bf523222e4aae43c229
c3=0x16c7c51ebd1e420ef58c4c675c0528043f021af620e0e57cc781714c737684df21782295fc343d44a52b938788438b8880c93b

def broadcast(n1, n2 ,n3, c1, c2, c3):
    n = [n1, n2, n3]
    C = [c1, c2, c3]
    N = 1
    for i in n:
        N *= i
    Ni = []
    for i in n:
        Ni.append(N / i)
    T = []
    for i in xrange(3):
        T.append(long(invert(Ni[i], n[i])))
    X = 0
    for i in xrange(3):
        X += C[i] * Ni[i] * T[i]
    m3 = X % N
    m = iroot(m3, 3)
    return m[0]

print(hex(broadcast(n1, n2 ,n3, c1, c2, c3)))
```

第五问

```
[+++++]challenge 4 completed[+++++]
[+]Generating challenge 5
[+]n=0x2030ca024a23fb978752ccc2897947fd9c82b682915771e447fc1ee6a6be8cbcc00df7cc2dfc401516b88b06a044b6fa595c
[+]e=3
[+]m=random.getrandbits(512)
[+]c=pow(m,e,n)=0x45204e3e2d780d6fded3ed4c53ca2a0300a78bd7f9b30afb5e3267bcb7074756ab386a165cf0678e3af272151
[+]x=pow(m+1,e,n)=0x1c17423e4aa0ee916c513f9f6f7f7f6efda060974ad06282bd846a50571c2b26465aba50a48eda745b0bb5b
[-]long_to_bytes(m).encode('hex')
```

高位相同的m

短填充攻击Coppersmith Shortpad Attack

参考脚本<https://github.com/ValarDragon/CTF-Crypto/blob/master/RSA/FranklinReiter.sage>

```

#sage
def franklinReiter(n,e,r,c1,c2):
    R.<X> = Zmod(n)[]
    f1 = X^e - c1
    f2 = (X + r)^e - c2
    # coefficient 0 = -m, which is what we wanted!
    return Integer(n-(compositeModulusGCD(f1,f2)).coefficients()[0])

# GCD is not implemented for rings over composite modulus in Sage
# so we do our own implementation. Its the exact same as standard GCD, but with
# the polynomials monic representation
def compositeModulusGCD(a, b):
    if(b == 0):
        return a.monic()
    else:
        return compositeModulusGCD(b, a % b)

def CoppersmithShortPadAttack(e,n,C1,C2,eps=1/30):
    """
    Coppersmith's Shortpad attack!
    Figured out from: https://en.wikipedia.org/wiki/Coppersmith's\_attack#Coppersmith.E2.80.99s\_short-pad\_at
    """
    P.<x,y> = PolynomialRing(ZZ)
    ZmodN = Zmod(n)
    g1 = x^e - C1
    g2 = (x+y)^e - C2
    res = g1.resultant(g2)
    P.<y> = PolynomialRing(ZmodN)
    # Convert Multivariate Polynomial Ring to Univariate Polynomial Ring
    rres = 0
    for i in range(len(res.coefficients())):
        rres += res.coefficients()[i]*(y^(res.exponents()[i][1]))

    diff = rres.small_roots(epsilon=eps)
    recoveredM1 = franklinReiter(n,e,diff[0],C1,C2)
    print(recoveredM1)
    print("Message is the following hex, but potentially missing some zeroes in the binary from the right e
    print(hex(recoveredM1))

eps=1/25
e=3
n=0x2030ca024a23fb978752ccc2897947fd9c82b682915771e447fc1eefa6be8cbcc00df7cc2dfc401516b88b06a044b6fa595ce67
c1=0x45204e3e2d780d6fdded3ed4c53ca2a0300a78bd7f9b30afb5e3267bcb7074756ab386a165cf0678e3af272151b0635c784df30
c2=0x1c17423e4aa0ee916c513f9f6f7f7f6efda060974ad06282bd846a50571c2b26465aba50a48eda745b0bb5b410d0b89a199256
CoppersmithShortPadAttack(e,n,c1,c2,eps)

```

第六问

```
[+++++]challenge 5 completed[+++++]
[+]Generating challenge 6
[+]n=0xbadd260d14ea665b62e7d2e634f20a6382ac369cd44017305b69cf3a2694667ee651acded7085e0757d169b090f29f3f86fe
[+]d=random.getrandbits(1024*0.270)
[+]e=invmod(d,phin)
[+]hex(e)=0x11722b54dd6f3ad9ce81da6f6ecb0acaf2cbc3885841d08b32abc0672d1a7293f9856db8f9407dc05f6f373a2d92467
[+]m=random.getrandbits(512)
[+]c=pow(m,e,n)=0xe3505f41ec936cf6bd8ae344bfec85746dc7d87a5943b3a7136482dd7b980f68f52c887585d1c7ca099310c4d
[-]long_to_bytes(m).encode('hex')=
```

e很大， $d < N$ 的0.292次方

使用Boneh and Durfee attack

参考<https://cryptologie.net/article/241/implementation-of-boneh-and-durfee-attack-on-rsas-low-private-exponents/>

https://github.com/mimoo/RSA-and-LLL-attacks/blob/master/boneh_durfee.sage

这题脚本太长了，不贴了，跟github的几乎一样，解

得d=7767654550817953771173776802095102348872301293185750633826345933577249982075

总结

第一问答案

258aa871ef627602f03f2100efe0c045d4a307153ca71f26e22fc2bcb72a16ae695d5bad767d258aa42e02a5c6b270a8c355c8a3588

第二问答案

5f3cef264c352ae60757725eb56469e601e740f88e6e62ad26aecb8623fa4d66a5cb135b759bc0eccafca69f1d2f9899ca207f15ae8

第三问答案

e862dec14b008fe307046a787af4f72865680fb141c734681fc923dc7206bb67693ed08146057d708eb3666b544b4a3386fffb241f0

第四题答案

dc419a862dd40cdc94e251f21c95fac5c28e3e86d629d748e881de3a5ea022c238b87a28889b506c22d488d3bdd6a2c6810087140c3

第五问答案

2d09b4627af9e9c4e118386ce6062c62638d7208f894d2117b3fc910af5bec88ffd84d35e965411cb4f2095a5b39e9e4eb2d13df5a8

第六问答案

6b3bb0cdc72a7f2ce89902e19db0fb2c0514c76874b2ca4113b86e6dc128d44cc859283db4ca8b0b5d9ee35032aec8cc8bb96e8c115

几乎都是coppersmith相关的攻击，第一次接触，没想到RSA还有这么多讲究，稍微不注意就可能被解密

randomstudy

```

import random
import time
import subprocess

def bye():
    print "[+]bye~"
    sys.exit()

def challenge1():
    print "[+]Generating challenge 1"
    random.seed(int(time.time()))
    for i in range(200):
        recv=int(raw_input("[-]"))
        if recv==random.randint(0,2**64):
            print "[++++++++++++]challenge 1 completed[++++++++++++]"
            return
        else:
            print "[+]failed"
    bye()

def challenge2():
    print "[+]Generating challenge 2"
    for i in range(200):
        o = subprocess.check_output(["java", "Main"])
        tmp=[]
        for i in o.split("\n")[0:3]:
            tmp.append(int(i.strip()))
        v1=tmp[0] % 0xffffffff
        v2=tmp[1] % 0xffffffff
        v3=tmp[2] % 0xffffffff
        print "[-]+"str(v1)
        print "[-]+"str(v2)
        v3_get=int(raw_input("[-]"))
        if v3_get==v3:
            print "[++++++++++++]challenge 2 completed[++++++++++++]"
            return
        else:
            print "[+]failed"
    bye()

def challenge3():
    print "[+]Generating challenge 3"
    for i in range(1000):
        a=raw_input("[-]")
        target=random.getrandbits(32)
        if a!=str(target):
            print "[+]failed:"+str(target)
        else:
            print "[++++++++++++]challenge 3 completed[++++++++++++]"
            return
    bye()

```

nc 119.3.245.36 23456

第一步也是要破解一个sha256，跟上题的脚本一样

第一问

python生成随机数

由于`random.seed(int(time.time()))`中

时间可以猜测，故随机数种子可以猜测，则随机数可以猜测

输入队伍token前先等等，同时本地一起执行脚本，服务器时间和我本机时间相差约1到2秒

```
#python3
import random
import time

t = int(time.time())
print(f'now is {t}')
for i in range(-5,1):
    print(t+i,end=' ')
    random.seed(t+i)
    for j in range(10):
        print(random.randint(0,2**64),end=' ')
    print('')
```

```
(base) C:\Users\win10\Desktop\task_attach_klasMrd>python ran.py
now is 1558779243
1558779238 15739103492071633018 7512349607070392501 2140010766658718173 9216975642080675879 2702091502194681713 17658477296392719461 6044959745144632154 14965672369637667322 707356
0930374189905 8766909699618931041
1558779239 7403864689634515398 3801543772499703988 3824703260119635747 13958055984064366790 6781516615343579367 9893654734608277396 16009195149560632789 13436768956912694491 163813
89400600433313 6728182182456407848
1558779240 12343910697068365394 5118742059170868508 5791619333813491256 110826534600867536 608883803988043985 11737255742579153175 2776727305697825426 9848703795483853719 13932832
629363123499 8690982726503491625
1558779241 7785400769138624261 18310899697053452148 6195007737575231657 13483410299966587467 15778890052213800780 5212225370691051888 4191614485709584259 1414033104265296042 897849
4748343153302 12817599001453985228
1558779242 3152575183136638643 8325488681982927764 12702162143381731027 875031783277696589 16643484688754534044 6577654086512834311 6909275928872832768 2483756901597317833 10917874
204665833194 299545128876560372
1558779243 308817274180582851 11234394670723151417 8393790580302814656 14439535756794835600 8134063463880972633 8477253976246613067 4221905822134388927 8294215938166598623 17479588
550314125624 3939958054315610755
```

时间脚本

先猜测最后一行第二列，再猜测倒数第二行第三列，以此类推，同时记录猜测次数和猜对后的时间种子，第三问要用

第二问

java的随机数破解

```
[+++++++++]challenge 1 completed[+++++++++]
[+]Generating challenge 2
[-]44003964
[-]977222536
```

同时附件里有份Main.class，可知是python调用java运行了Main.class

用<http://www.javadecompilers.com>在线反编译，可以得到源码

```
import java.util.Random;

public class Main { public Main() {}
    public static void main(String[] paramArrayOfString) {
        Random localRandom = new Random();
        System.out.println(localRandom.nextInt());
        System.out.println(localRandom.nextInt());
        System.out.println(localRandom.nextInt());
    }
}
```

参考这篇文章

https://jazzy.id.au/2010/09/20/cracking_random_number_generators_part_1.html

代码参考

<https://github.com/sacundim/cracking-prngs/blob/master/src/main/java/org/casillas/Main.java>

题目给出前两个随机数，要求猜测第三个

在java中，seed是48位，nextInt()返回32位，如果能拿到两个nextInt()，就能反推出seed

脚本如下，修改变量v1，v2

因为题目给的数字经过了转化，类似于int转unsigned int，要先转换一下再带入脚本，或者看运气，等给出了两个比较小的int(捂脸)

```
a=977222536
print(a if a<0x7fffffff else -1*(a&0x7fffffff))
```

```
package org.casillas;

import java.util.Random;

/**
 * A simple program demonstrating how easy it is to predict the output of {@link java.util.Random}. Based
 * code here, but refactored a bit, and updated to Java 8:
 *
 * <ul>
 * <li>https://jazzy.id.au/2010/09/20/cracking\_random\_number\_generators\_part\_1.html</li>
 * </ul>
 */
public class Main {
    // These three values come from `java.util.Random`. Note that these changed between Java 6 and 7.
    private static final long multiplier = 0x5DEECE66DL;
    private static final long addend = 0xBL;
    private static final long mask = (1L << 48) - 1;

    public static void main(String[] args) {
        Random target = new Random();
        int v1 = target.nextInt();
        int v2 = target.nextInt();
        long seed = guessSeed(v1, v2);
        System.out.printf("Guessed seed: 0x%016x. Testing...\n", seed);
        testGuess(seed, target, v2);
        System.out.println("Success!!!");
    }

    /**
     * We can guess the state of the generator just from observing two consecutive {@code int}s.
     */
    private static long guessSeed(int v1, int v2) {
        System.out.printf("v1 = 0x%08x, v2 = 0x%08x\n", v1, v2);
        return guessSeed(maskToLong(v1), maskToLong(v2));
    }

    private static long guessSeed(long v1, long v2) {
        for (int i = 0; i < 65536; i++) {
            long guess = v1 * 65536 + i;
            if (((guess * multiplier + addend) & mask) >>> 16) == v2) {
                return (guess ^ multiplier) & mask;
            }
        }
    }
}
```

```

    }
}
throw new IllegalStateException("CAN'T HAPPEN: Could not guess the seed!");
}

/**
 * Convert an int to a long in a way that preserves all the bits (negative numbers/twos complement issue)
 */
private static long maskToLong(int n) {
    return n & 0x00000000ffffffffL;
}

private static void testGuess(long seed, Random target, int expected) {
    Random experiment = new Random(seed);
    int actual = experiment.nextInt();
    for (int i = 0; i < 100_000; i++) {
        if (actual != expected) {
            // This will never actually happen.
            String msg = "i = %d, expected = 0x%08x, actual = 0x%08x";
            throw new IllegalStateException(String.format(msg, i, expected, actual));
        }
        expected = target.nextInt();
        actual = experiment.nextInt();
    }
}
}
}

```

同样，得到的数字可能是负数，转换一下

```
print(-2145376347 % 0xffffffff)
```

第三问

比第一问简单，就是要记录一下第一问的情况
输入第一问得到的种子，并输入第一问时的尝试次数

```

import random
import time

s = input("seed=")
random.seed(int(s))
ci = input("cishu=")
for i in range(int(ci)):
    print(random.randint(0,2**64),end=',')
print('')
print(random.getrandbits(32))

```

```

flag=open("flag","rb").read()

from Crypto.Util.number import getPrime,bytes_to_long
p=getPrime(1024)
q=getPrime(1024)
e=65537
n=p*q
m=bytes_to_long(flag)
c=pow(m,e,n)
print c,e,n

p=getPrime(1024)
e=65537
n=p*q
m=bytes_to_long("1"*32)
c=pow(m,e,n)
print c,e,n

...
output:
24820838937466182485444267370237504001245434520824363343985049860235017106394020609491066932794628969688390
38290600395720427374966791868810679503289561331636299088723481081601295504376976771505994839239257982243281
...

```

相比起copperstudy, 这就是送分题了

两个 n_1, n_2 使用了同一个因子 p , 求一下 n_1, n_2 的最大公约数就得到 p 了

$q=n_1/p$

```

import gmpy2
import libnum
c1=24820838937466182485444267370237504001245434520824363343985049860235017106394020609491066932794628969688
e1=65537
n1=14967030059975114950295399874185047053736587880127990542035765201425779342430662517765063258784685868107
c2=38290600395720427374966791868810679503289561331636299088723481081601295504376976771505994839239257982243
e2=65537
n2=14624662628725820618622370803948630854094687814338334827462870357582795291844925274690253604919535785934

p=gmpy2.gcd(n1,n2)
assert n1%p==0
q1=n1/p
q2=n2/p

phin1=(p-1)*(q1-1)
d1=gmpy2.invert(e1,phin1)
m1=pow(c1,d1,n1)
print(libnum.n2s(m1))

```

flag{i_am_very_sad_233333333333}

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